

## Chapter 5: Electric Forces and Fields

### Background/Summary:

This chapter is all about electric *charges*, which can be positive or negative. The basic principle is that like charges repel each other while opposites attract.

What forces do they exert on each other? What are the electric fields that they produce (point charge vs. continuous)? How are they acted on by electric fields?

### Major Topics (Including **Formulae** & When to Use):

**Coulomb's Law:** two charges will exert forces on each other that are identical in magnitude.

$$|\vec{F}_E| = k \left| \frac{q_1 q_2}{r^2} \right| \quad * \text{unit: Newtons}$$

force of  $q_1$  on  $q_2$  or vice versa  
 $\frac{1}{4\pi\epsilon_0} = 8.99e9 \frac{N \cdot m^2}{C^2}$   
 meters between 2 charges

- direction can be represented by unit vector  $\hat{r}$  that points from  $q_1$  to  $q_2$ 
  - $q_1$  &  $q_2$  have different signs  
 $\rightarrow \ominus = \text{attraction}$
  - $q_1$  &  $q_2$  have same sign  
 $\rightarrow \oplus = \text{repulsion}$
- electrons vs. protons have charges of
  - $-1.602e-19$  Coulomb
  - $+1.602e-19$  C

If charges are not aligned on a single axis, a 2-dimensional analysis is needed. Apply Coulomb's Law to each force, break forces into their component parts if applicable, and then add the like component parts together (ex: x-components) to get the component vectors of the net force.

Resources: crashwhite.com and openstax University Physics Volume 2 textbook

**Electric Fields & Charges in Electric Fields:** point charges, which theoretically have no mass and thus exist at a single point, produce electric fields. The direction of an electric field is the same direction as the source charge's force on a positive charge. Thus, if the source charge is positive, its electric field points away from it. If the source charge is negative, its electric field points towards it.

$$\vec{E} = \frac{\vec{F}_e}{Q} = \frac{kq}{r^2} \hat{r}$$
 (can use  $F_{net} = ma$ )

$$\frac{F_e}{Q} = \frac{kqQ}{Qr^2} = \frac{kq}{r^2}$$
 (use if don't know source)

\* unit : Newtons / Coulomb

- Q doesn't affect the magnitude of E, but it does determine the direction of  $F_e$

A positive charge experiences a force in the same direction as the electric field while a negative charge experiences a force in the OPPOSITE direction as the electric field.

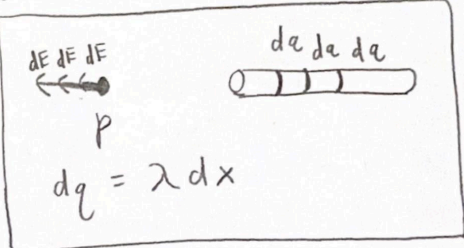
**Electric Field of Continuous Charges:** continuous charges also produce electric fields, but we have to use calculus to solve for theirs. Imagine the continuous charge as a sum of its infinitesimal portions, called  $dq$ . Each  $dq$  produces an infinitesimal portion of an electric field,  $dE$ , which can be quantified with the equation we derived earlier of  $E = \frac{kq}{r^2}$  except  $q$  is  $dq$ .

Adding all the  $dE$ s through an integral gives us the net electric field. To solve this integral, we can use the charge density relationships below and substitution.

Resources: crashwhite.com and openstax University Physics Volume 2 textbook

$$\vec{E} = \int k \frac{dq}{r^2} \hat{r}$$
 radial direction  
 $\ominus =$  toward source charge  
 $8.99e9 \frac{N \cdot m^2}{C^2}$   
 distance between charge and E at point P

Linear:  $\lambda = \frac{q}{L} \rightarrow dq = \lambda dL$  or  $dx$   
 Area:  $\sigma = \frac{q}{A} \rightarrow dq = \sigma dA$   
 Volume:  $\rho = \frac{q}{V} \rightarrow dq = \rho dV$



The diagram shows a horizontal rod with three segments labeled  $da$ . To the left of the rod, a point  $P$  is marked. Three arrows labeled  $dE$  point from the rod segments towards point  $P$ . Below the diagram, the equation  $dq = \lambda dx$  is written.

**Vocabulary:**

- **conductor:** made of metal. Conducts charge easily.
- **insulator:** rubber, plastic, wood, etc. Does not conduct charge easily because electrons are more tightly bound to the nucleus of atoms.
- **conduction:** occurs when two conductors with different charges make contact, resulting in the swapping of electrons
- **induction:** an object with a charge near a neutral conductor causes the conductor to become polarized

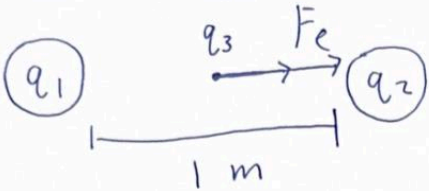
**Problems in Order of Difficulty (Easy, Medium, Hard):**

**73.** If the electric field is  $100 \text{ N/C}$  at a distance of  $50 \text{ cm}$  from a point charge  $q$ , what is the value of  $q$ ?

$$73. E = \frac{kq}{r^2} \rightarrow 100 = \frac{(8.99e9)q}{(0.5)^2} \rightarrow \boxed{q = 2.78e-9 \text{ C}}$$

**53.** Point charges  $q_1 = 50 \mu\text{C}$  and  $q_2 = -25 \mu\text{C}$  are placed  $1.0 \text{ m}$  apart. What is the force on a third charge  $q_3 = 20 \mu\text{C}$  placed midway between  $q_1$  and  $q_2$ ?

53.



$q_1 = 50 \text{ nC}$      $q_2 = -25 \text{ nC}$      $q_3 = 20 \text{ nC}$

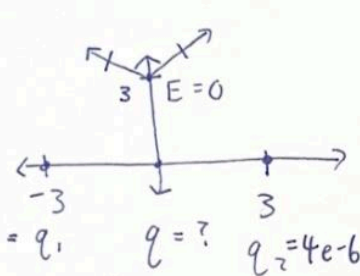
$F_{e_{2-3}} = k \frac{q_1 q_2}{r^2} = (8.99 \text{ e9}) \frac{(-25 \text{ e-6})(20 \text{ e-6})}{(0.5)^2} = 18.0 \text{ N, attraction}$

$F_{e_{1-3}} = k \frac{q_1 q_2}{r^2} = (8.99 \text{ e9}) \frac{(50 \text{ e-6})(20 \text{ e-6})}{(0.5)^2} = 36.0 \text{ N, repulsion}$

$F_{\text{net}} = F_{e_{2-3}} + F_{e_{1-3}} = 18 + 36 = \boxed{54.0 \text{ N, right}}$

**79.** Point charges  $q_1 = q_2 = 4.0 \times 10^{-6} \text{ C}$  are fixed on the  $x$ -axis at  $x = -3.0 \text{ m}$  and  $x = 3.0 \text{ m}$ . What charge  $q$  must be placed at the origin so that the electric field vanishes at  $x = 0, y = 3.0 \text{ m}$ ?

79.



$4 \text{ e-6} = q_1$      $q = ?$      $q_2 = 4 \text{ e-6}$

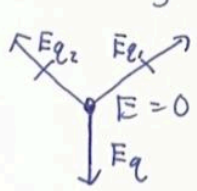
- $x$  components of  $E$  from  $q_1$  and  $q_2$  cancel, but the  $y$ -components add up
- first, we need to find the magnitude of those  $y$ -components

$E = \frac{kq}{r^2} = (8.99 \text{ e9})(4 \text{ e-6})$   
 $E = 2000 \text{ N/C}$

$E_y = E \sin \theta$   
 $E_y = 2000 \sin(45^\circ)$   
 $E_y = 1414 \text{ N/C} \times 2 = 2.83 \text{ e3 N/C}$

$E = \frac{kq}{r^2} \rightarrow 2.83 \text{ e3} = \frac{(8.99 \text{ e9})q}{3^2} \rightarrow q = \boxed{-2.83 \text{ e-6 C}}$

$q$  is negative so that its  $E$  will cancel out the  $E$  upward



$a^2 + b^2 = c^2$   
 $c = 4.24$